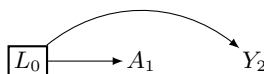


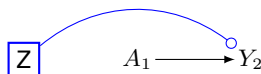
## Interest

## Causal Directed Acyclic Graph

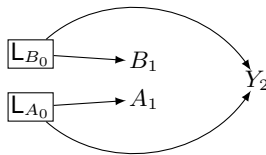
**Treatment effect:** after controlling for all common causes, what is the causal effect of  $A \rightarrow Y$ ?



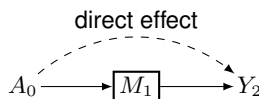
**Effect Modification (Moderation):** does the effect of  $A \rightarrow Y$  vary across levels of  $Z$ ?



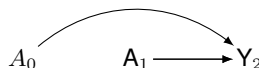
**Interaction (joint-intervention):** after controlling for all common causes of  $A \rightarrow Y$  and  $B \rightarrow Y$ , is the combined effect of  $A$  and  $B$  on  $Y$  different from their individual effects?



**Mediation:** assuming unbiased confounding control, what are the separable effects of  $A \rightarrow Y$  (a) indirectly through  $M$  and (b) directly not through  $M$ ?



**Time-varying exposures:** What are the causal effects of clearly specified sequential treatments?  $A \rightarrow Y$ ?



### Key:

$A$  denotes the treatment;

$B$  denotes a second treatment (as in interaction analysis).

$Y$  denotes the outcome;

$L$  denotes a confounder;

$Z$  denotes a modifier of for the effect of  $A \rightarrow Y$

$X$  indicates conditioning on variable  $X$ .

$\rightarrow$  asserts causality

$\rightarrow \circ$  indicates an interest in effect-modification (causality need not be asserted);

**Note 1:** when analysing effect-modification, our focus is on the  $A \rightarrow Y$  pathway, and whether this effect varies within levels of  $Z$ ; we do not estimate  $Z$ 's causal effect (if any) on  $Y$ . We use the agnostic arrow  $\rightarrow \circ$  to denote this specific interest in  $Z$  in relation to  $A \rightarrow Y$ .

**Note 2:** interaction analysis requires identifying two causal effects ( $A \rightarrow Y$  and  $B \rightarrow Y$ ) and controlling for their common causes. Mediation analysis, not interaction analysis, is needed if  $A$  and  $B$  influence each other ( $B \rightarrow A$  or  $A \rightarrow B$ ).